## DESCRIPTION OF THE COURSE OF STUDY

| Course code | 0541.6.MAT1.C.ATL |  |
| :--- | :---: | :---: |
| Name of the course in | Polish | Algebra z teorią liczb |
|  | English | Algebra and Number Theory |

## 1. LOCATION OF THE COURSE OF STUDY WITHIN THE SYSTEM OF STUDIES

| 1.1. Field of study | mathematics |
| :--- | :--- |
| 1.2. Mode of study | full-time studies |
| 1.3. Level of study | Undergraduate (Bachelor) |
| 1.4. Profile of study* | general academic profile of studies |
| 1.5. Person/s preparing the course description | dr Elżbieta Zając |
| 1.6. Contact | ezajac@ ujk.edu.pl |

2. GENERAL CHARACTERISTICS OF THE COURSE OF STUDY

| 2.1. Language of instruction | Polish and English |
| :--- | :--- |
| 2.2. Prerequisites* |  |

3. DETAILED CHARACTERISTICS OF THE COURSE OF STUDY

| 3.1. Form of classes | lectures / classes |
| :--- | :--- |
| 3.2. Place of classes | classes in the UJK teaching room |
| 3.3. Form of assessment | Exam (lectures), graded credit (classes) |
| 3.4. Teaching methods | Lectures - information lecture, discusions <br> Classes - discusions, solving problems |
| 3.5. Bibliography |  |
| Required reading |  |
| Kostrikin A.I., Introduction to algebra |  |
|  | Further reading |
|  |  |

4. OBJECTIVES, SYLLABUS CONTENT AND INTENDED LEARNING OUTCOMES
4.1. Course objectives (including form of classes)

C1. Introduction into abstract algebra methods including group theory, ring theory and fields
C2. Applying algebraic methods to number theory
C3. Developing the student skills of using algebraic methods and doing characterization of algebraic structures.

### 4.2. Detailed syllabus (including form of classes)

## Lectures

1. Groups, subgroups, cosets and Lagrange Theorem.
2. Normal subgroups, quotient groups, group homeomorphism and isomorphism, the group isomorphism theorem
3. Cyclic groups, abelian groups and solvable groups, direct sums of groups and their application
4. Permutation groups and Cayley's theorem
5. Rings, subrings ,ideals and ring homeomorphisms, the ring isomorphism theorem
6. Integral domains, divisibility, prime elements and factorization
7. Principal ideal domains, unique factorization domains and Euclidean domains
8. The ring of integers: the algebraic characterization, congruences,
9. Number theory: Euler theorem and its application, solving of some Diophantine equations
10. Polynomial rings, polynomial divisibility, irreducible polynomials, decomposition of polynomials, polynomial roots
11. Fields, subfields, field extension, algebraic extension of a field
12. Algebraically closed fields and fundamental theorem of algebra
13. Construction of finite fields

Classes

1. Example of group structures. Describing cosets of a group for a given subgroup. Applying of Lagrange theorem
2. Identifying normal subgroups of a group. Applying isomorphism theorem to characterize quotient groups.
3. Recognizing and characterizing cyclic, abelian and solvable groups. Using direct sums. Prooving some algebraic properties.
4. Identifying ring structures, their subrings and ideals, giving examples. Applying the ring isomorphism theorem to characterize a quotient ring.
5. Characterizing properties of some ring elements.
6.Characterizing some integral domains, proving that they are (or aren't) Euclidean "principal ideal" or "unique factorization
6. Describing congruences in the ring of integers, proving some rules of divisibility
7. Applying Euler theorem find a reminder in an integer division
8. Using Euclid algorithm to solve Diophantine equation ax+by=c
9. Describing polynomials, finding roots of a polynomial, polynomial factorization
10. Examples of fields and subfields,
11. Construction of finite fields
4.3 Intended learning outcomes

| تِ تِ | A student, who passed the course | Relation to learning outcomes |
| :---: | :---: | :---: |
| within the scope of KNOWLEDGE: |  |  |
| ...W01 | identifies an algebraic structure of a group, a rings or a field, describes the application of the basic theorems of the group theory, the ring theory and the field theory | MAT1A_W01 <br> MAT1A_W02 <br> MAT1A_W03 <br> MAT1A_W05 <br> MAT1A W11 |
| ...W02 | describes the application of algebraic methods in characterization algebraic structures and in solving some problems in number theory | MAT1A_W03 <br> MAT1A_W04 <br> MAT1A_W05 <br> MAT1A_W06 <br> MAT1A_W07 <br> MAT1A_W09 <br> MAT1A_W11 |
| within the scope of ABILITIES: |  |  |
| ...U01 | describes properties of an algebraic structure (group, ring or field) | MAT1A_U01 MAT1A_U02 MAT1A_U08 MAT1A_W11 |
| ...U02 | determines and characterizes quotient algebras (groups, rings) | MAT1A_U01 <br> MAT1A_U02 <br> MAT1A_U08 <br> MAT1A_W07 <br> MAT1A_W09 <br> MAT1A W1 |
| U03 | describes properties of a polynomial uses algebraic methods to solve some problems in number theory | $\begin{aligned} & \hline \text { MAT1A_U01 } \\ & \text { MAT1A_U02 } \\ & \text { MAT1A_U08 } \\ & \text { MAT1A_W07 } \\ & \text { MAT1A_W09 } \\ & \text { MAT1A_W11 } \\ & \hline \end{aligned}$ |
| within the scope of SOCIAL COMPETENCE: |  |  |
| ...K01 | asks precise questions to better understand the subject, develops own examples. | MAT1A_K02 |



## *delete as appropriate

### 4.5. Criteria of assessment of the intended learning outcomes

Form of classes $\qquad$ Criterion of assessment

|  | 3 | at least $50 \%$ and no more than $60 \%$ of the total number of points possible |
| :---: | :---: | :---: |
|  | 3,5 | more than $60 \%$ and no more than $70 \%$ of the total number of points possible |
|  | 4 | more than $70 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 4,5 | more than $80 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 5 | more than $90 \%$ of the total number of points possible |
|  | 3 | at least $50 \%$ and no more than $60 \%$ of the total number of points possible |
|  | 3,5 | more than $60 \%$ and no more than $70 \%$ of the total number of points possible |
|  | 4 | more than $70 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 4,5 | more than $80 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 5 | more than $90 \%$ of the total number of points possible |
|  | 3 | at least $50 \%$ and no more than $60 \%$ of the total number of points possible |
|  | 3,5 | more than $60 \%$ and no more than $70 \%$ of the total number of points possible |
|  | 4 | more than $70 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 4,5 | more than $80 \%$ and no more than $80 \%$ of the total number of points possible |
|  | 5 | more than $90 \%$ of the total number of points possible |

## 5. BALANCE OF ECTS CREDITS - STUDENT'S WORK INPUT

| Category | Student's workload |  |
| :---: | :---: | :---: |
|  | Full-time studies | Extramural studies |
| NUMBER OF HOURS WITH THE DIRECT PARTICIPATION OF THE TEACHER /CONTACT HOURS/ |  |  |
| Participation in lectures* | 45 |  |
| Participation in classes, seminars, laboratories* | 45 |  |
| Preparation in the exam/ final test* | 2 |  |
| Others (please specify e.g. e-learning)* |  |  |
| INDEPENDENT WORK OF THE STUDENT/NON-CONTACT HOURS/ | 83 |  |
| Preparation for the lecture* | 13 |  |
| Preparation for the classes, seminars, laboratories* | 40 |  |
| Preparation for the exam/test* | 30 |  |
| Gathering materials for the project/Internet query* |  |  |
| Preparation of multimedia presentation |  |  |
| Others * |  |  |
| TOTAL NUMBER OF HOURS | 175 |  |
| ECTS credits for the course of study | 7 |  |

*delete as appropriate
Accepted for execution (date and legible signatures of the teachers running the course in the given academic year)

