# **DESCRIPTION OF THE COURSE OF STUDY**

Course code		0541.6.MAT1.C.WGR							
Name of the course in	Polish Wstęp do geometrii różniczkowej								
	English	Introduction to Differential Geometry							

#### 1. LOCATION OF THE COURSE OF STUDY WITHIN THE SYSTEM OF STUDIES

1.1. Field of study	mathematics
1.2. Mode of study	full-time studies
1.3. Level of study	Undergraduate (Bachelor)
1.4. Profile of study*	general academic profile of studies
1.5. Person/s preparing the course description	dr Michał Zakrzewski
1.6. Contact	zakrzewski@mimuw.edu.pl

# 2. GENERAL CHARACTERISTICS OF THE COURSE OF STUDY

2.1. Language of instruction	Polish and English
2.2. Prerequisites*	Mathematical Analysis III and IV, Linear Algebra and Ge-
	ometry

### 3. DETAILED CHARACTERISTICS OF THE COURSE OF STUDY

3.1.	Form of classes		lectures and classes				
3.2.	Place of classes		classes in the UJK teaching room				
3.3.	Form of assessn	nent	Exam (lectures), graded credit (classes)				
3.4.	Teaching metho	ds	Lectures – information lecture				
	0		Classes - discusions, solving problems				
3.5.	Bibliography	<b>Required reading</b>	1. Oprea J. Geometria różniczkowa i jej zastosowania, Wydawnictwo Naukowe				
	0.0	•	PWN, 2002.				
			2. Petersen P. Classical Differential Geometry. Available at:				
			http://www.math.ucla.edu/~petersen/DGnotes.pdf				
			3. Panasyuk A. Wyklady z geometrii rożniczkowej. Available at:				
			http://wmii.uwm.edu.pl/~panas/talks/geomrozn.pdf				
		Further reading	1.) Aubin T. A Course in Differential Geometry, AMS, 2001.				
		0	2.) Dubrovin B., Fomenko A., Novikov, S. P.; Modern Geometry t. I i II,				
			Springer GTM 93 i 104, 1984 – 1985.				
			3.) Petersen P.; Manifold Theory. Available at:				
			http://www.math.ucla.edu/~petersen/manifolds.pdf				

#### 4. OBJECTIVES, SYLLABUS CONTENT AND INTENDED LEARNING OUTCOMES

## 4.1. Course objectives (including form of classes)

Lecture

C1 - basics of differential geometry

C2 - introduction to the elements of the theory of curves and surfaces

C3 - basics of modern abstract differential geometry

Classes

C1 - problems concerning curves and embedded surfaces

C2 - to develop the habit of learning, improving one's own work and formulating questions to deepen one's own

understanding of differential geometry

# 4.2. Detailed syllabus (including form of classes)

### Lectures

Vector calculus, geometry in space with scalar product.  $R^2$  and  $R^3$  symmetry groups. Curves and surfaces as simplest manifolds. Differential forms. Riemann metric on a surface. Curvature of a surface. Gauss's Theorema Egregium and Gauss-Bonnet theorem. Mean curvature and minimal surfaces. Remarks on general Riemannian geometry and its applications.

### Classes

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#### 4.3 Intended learning outcomes

e		<b>Relation to learning</b>
oo	A student, who passed the course	outcomes
0		

within the scope of <b>KNOWLEDGE</b> :									
W01	formulates basic theorems about curves and embedded surfaces	MAT1A_W01							
		MAT1A_W02							
		MAT1A_W03							
		MAT1A W04							
		MAT1A W05							
		MAT1A_W11							
W02	gives definitions of scalar product, diffeomorphism, smooth transformation, metric tensor, patch	MAT1A W01							
		MAT1A W02							
		MAT1A W03							
		MAT1A W04							
		MAT1A W05							
		MAT1A W11							
	within the scope of <b>ABILITIES</b> :								
U01	calculates the curvature and torsion of a smooth curve	MAT1A_U01							
		MAT1A_U02							
		MAT1A_U08							
U02	calculates Gaussian curvature and mean curvature	MAT1A_U01							
		MAT1A_U02							
		MAT1A_U08							
U03	uses the concepts of metric tensor and differential form and knows their applications in geometry	MAT1A_U01							
		MATIA_U02							
		MATIA_U08							
U04	Knows the basic relationships between geometry and topology of curves and surfaces	MATIA_U01							
		MATIA_U02							
	MAT1A_U08								
	within the scope of <b>SOCIAL COMPETENCE</b> :								
K01	Analyzes the logical accuracy of his own and other people's speech, strives for precision in writ-	MAT1A_K01							
	ing down text	MAT1A_K02							
K02	Strives to fully understand issues by asking appropriate questions.	MAT1A_K02							

4.4. Methods of assessment of the intended learning outcomes																					
	Method of assessment (+/-)																				
Teaching outcomes	Exam oral/written*			Test*			Project*			Effort in class*			Self-study*			Group work*			Others* e.g. standard- ized test used in e- learning		
(code)	F	Form o classe	of s	Form of classes			F	Form of classes			Form of classes			Form of classes			Form of classes			Form of classes	
	L	С		L	С		L	С		L	С		L	С		L	С		L	С	
W01	+				+					+	+		+	+							
W02	+				+					+	+		+	+							
W03	+				+					+	+		+	+							
U01					+					+	+		+	+							
U02					+					+	+		+	+							
U03					+					+	+		+	+							
U04					+					+	+		+	+							
K01	+				+					+	+		+	+							
K02	+									+	+		+	+							

\*delete as appropriate

4.5. Criteria of assessment of the intended learning outcomes									
Form of classes	Grade	Criterion of assessment							
<b>•</b>	3	at least 50% and no more than 60% of the total number of points possible							
🚽 ີ ຍັ ອີ 3,5		more than 60% and no more than 70% of the total number of points possible							
ure udi rni	4	more than 70% and no more than 80% of the total number of points possible							
lect inclu lea	4,5	more than 80% and no more than 90% of the total number of points possible							
I (i	5	more than 90% of the total number of points possible							

× !	3	at least 50% and no more than 60% of the total number of points possible
ng e ng e	3,5	more than 60% and no more than 70% of the total number of points possible
ses ( udin rnin	4	more than 70% and no more than 80% of the total number of points possible
lass nch lea	4,5	more than 80% and no more than 90% of the total number of points possible
c (j	5	more than 90% of the total number of points possible

# 5. BALANCE OF ECTS CREDITS – STUDENT'S WORK INPUT

	Student's workload					
Category	Full-time	Extramural studies				
	studies					
NUMBER OF HOURS WITH THE DIRECT PARTICIPATION OF THE TEACHER	65					
Participation in Lectures*	20					
Function in lectures	50					
Participation in classes, seminars, laboratories*	30					
Preparation in the exam/ final test*	3/2					
INDEPENDENT WORK OF THE STUDENT/NON-CONTACT HOURS/	35					
Preparation for the lecture*	10					
Preparation for the classes, seminars, laboratories*	15					
Preparation for the exam/test*	5/5					
TOTAL NUMBER OF HOURS	100					
ECTS credits for the course of study	4					

\*delete as appropriate

Accepted for execution (date and legible signatures of the teachers running the course in the given academic year)

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